



CHEMICAL EQUILIBRIUM

6.2 Equilibrium Constants (Part I)

At the end of the lesson, students should be able to:

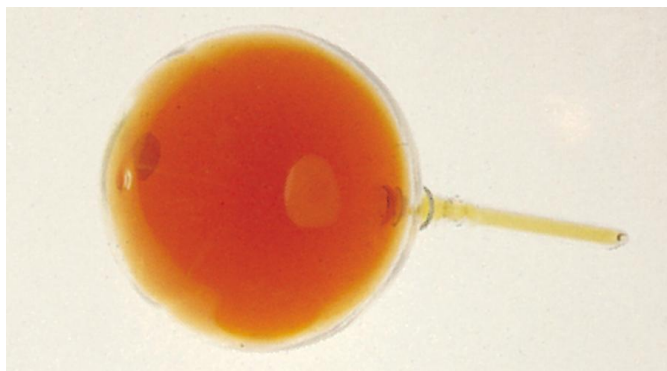
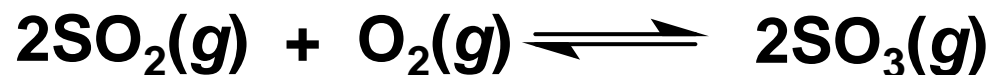
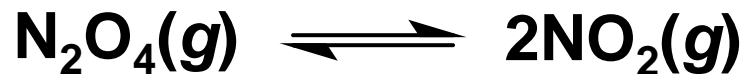
- (a) Define homogeneous and heterogeneous equilibria.
- (b) Deduce and write expressions for equilibrium constants in terms of concentration, K_c and partial pressure, K_p for homogeneous and heterogeneous systems.
- (c) Derive and use the equation, $K_p = K_c (RT)^{\Delta n}$.

LESSON DURATION: 1 hour



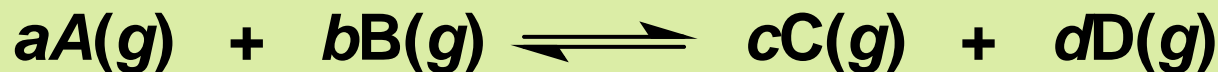
HOMOGENEOUS EQUILIBRIUM

👉 Products and reactants are in the **same phase**.





WRITING K_p AND K_c EXPRESSIONS



$$K_c = \frac{[C]^c [D]^d}{[A]^a [B]^b}$$

Subscript C in K_c =
concentrations of the
reacting species



$$K_c = \frac{[NO_2]^2}{[N_2O_4]}$$

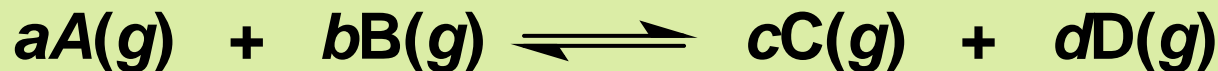


$$K_c = \frac{[CH_3COO^-][H^+]}{[CH_3COOH]}$$

Note: Unit of concentration = **M (mol L⁻¹)**



WRITING K_p AND K_c EXPRESSIONS

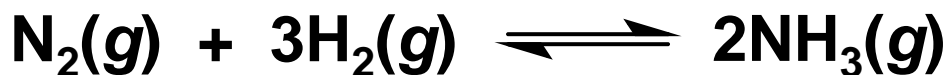


$$K_p = \frac{P_C^c P_D^d}{P_A^a P_B^b}$$

P = equilibrium partial pressure of the gas



$$K_p = \frac{P_{NO_2}^2}{P_{N_2O_4}}$$



$$K_p = \frac{P_{NH_3}^2}{P_{N_2} \times P_{H_2}^3}$$

Note:

Equilibrium constant expression (K_c or K_p) also called **Equilibrium law expression**

Note: Unit of pressure = **atm.**



WRITING K_p AND K_c EXPRESSIONS

$$PV = nRT$$

So

$$P = \frac{n}{V} RT \quad \text{or} \quad \frac{P}{RT} = \frac{n}{V}$$

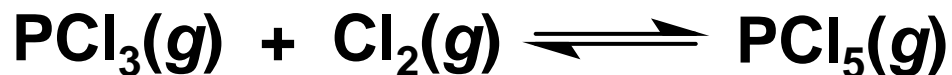
At constant temperature, pressure is **directly proportional** to molar concentration (n/V).



The **equilibrium constant** for reaction involving **gases**, can be expressed based on **concentrations** (K_c) and **pressures** (K_p).

Keep in mind!

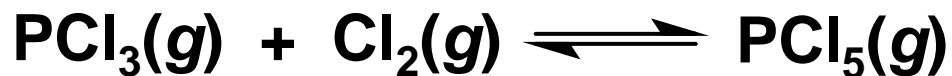
The equilibrium constant (K_C and K_P) is a **dimensionless** (no unit) quantity.



$$K_C = 1.67 \text{ (at 500K)}$$

$$K_P = 4.07 \times 10^{-2} \text{ (at 500K)}$$

Keep in mind!



$$K_C = 1.67 \text{ (at 500K)}$$

$$K_P = 4.07 \times 10^{-2} \text{ (at 500K)}$$

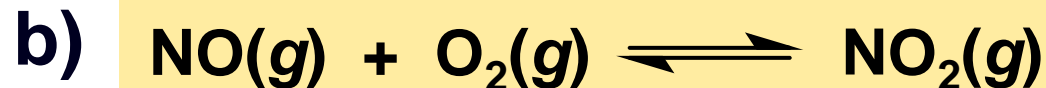
In quoting a value for the K_P or K_C , you **MUST** specify the balanced equation (including the phase of each reactant/product) and the temperature.



EXERCISE - 2

Write expressions for K_C , and K_p if applicable, for the following reversible reactions at equilibrium:

Note: balance the equations first.





EXAMPLE - 1

ANS:

The following equilibrium process has been studied at 230°C:



In one experiment the concentration of the reacting species at equilibrium are found to be $[\text{NO}] = 0.0542 \text{ M}$, $[\text{O}_2] = 0.127 \text{ M}$, and $[\text{NO}_2] = 15.5 \text{ M}$. Calculate the equilibrium constant (K_c) of the reaction at this temperature.

$$K_c = \frac{[\text{NO}_2]}{[\text{NO}]^2[\text{O}_2]} = \frac{(15.5)^2}{(0.0542)^2 \times 0.127} = 6.44 \times 10^5$$



EXERCISE - 3

Consider the following equilibrium process at 700°C:

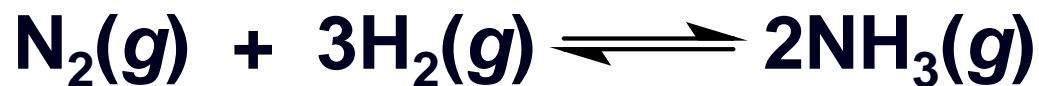


Analysis shows that at equilibrium, there are 2.50 mol of H_2 , 1.35×10^{-5} mol of S_2 , and 8.70 mol of H_2S present in a 12.0-L flask. Calculate the equilibrium constant K_C for the reaction.



EXERCISE - 4

At a certain temperature, $K_c = 1.8 \times 10^4$ for the reaction



If the equilibrium concentrations of N_2 and NH_3 are 0.015 M and 2.00 M, respectively, what is the equilibrium concentrations of H_2 ?



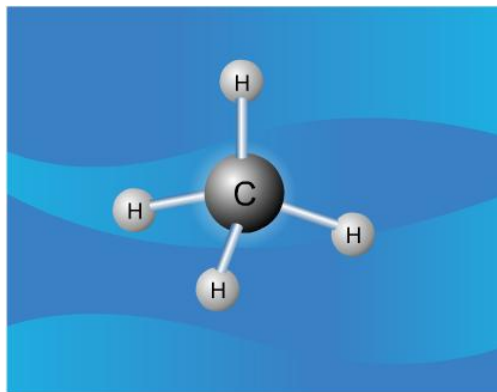
EXERCISE - 5

In a study of the conversion of methane to other fuels, a chemical engineer mixes gaseous CH_4 and H_2O in a 0.32-L flask at 1200 K.

At equilibrium, the flask contains 0.26 mol of CO , 0.091 mol of H_2 , and 0.041 mol of CH_4 .

What is $[\text{H}_2\text{O}]$ at equilibrium?

$K_C = 0.26$ for the equation



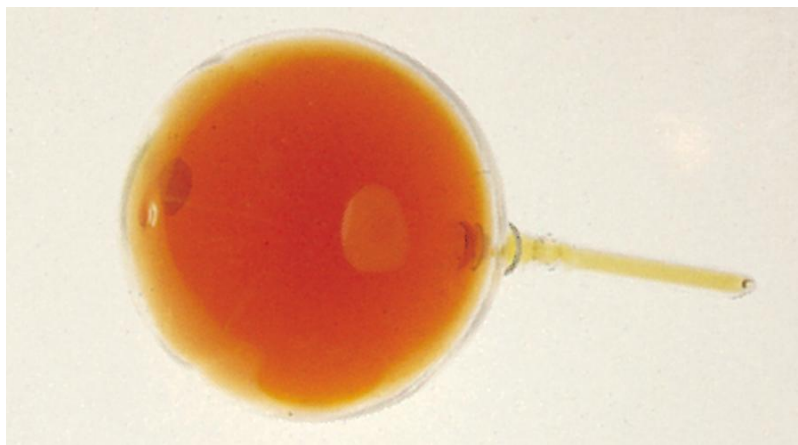


EXERCISE - 6

Equilibrium is established at 25°C in the reaction



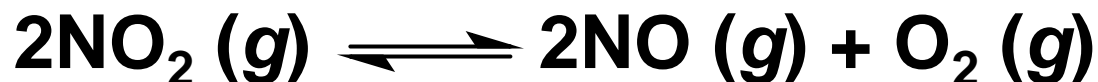
If $[\text{NO}_2] = 0.0236 \text{ M}$ in a 2.26-L flask, how many grams of N_2O_4 are also present?





EXAMPLE - 2

The equilibrium constant K_p for the reaction



is 158 at 1000K. What is the equilibrium pressure of O_2 if the $P_{\text{NO}_2} = 0.400$ atm and $P_{\text{NO}} = 0.270$ atm?

ANS:

$$K_p = \frac{P_{\text{NO}}^2 P_{\text{O}_2}}{P_{\text{NO}_2}^2}$$

$$P_{\text{O}_2} = K_p \frac{P_{\text{NO}_2}^2}{P_{\text{NO}}^2}$$

$$P_{\text{O}_2} = 158 \times (0.400)^2 / (0.270)^2 = 346.8 \text{ atm}$$

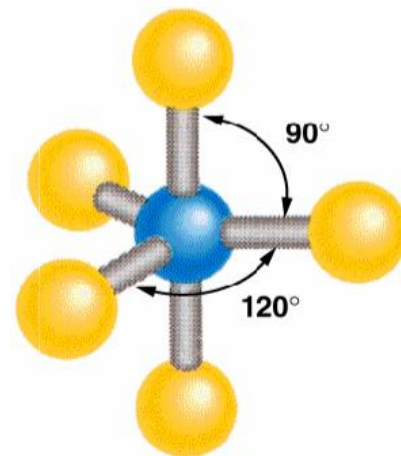


EXERCISE - 7

The equilibrium constant K_p for the decomposition of phosphorus pentachloride to phosphorus trichloride and molecule chlorine



is found to be 1.05 at 250°C. If the equilibrium partial pressure of PCl_5 and PCl_3 are 0.875 atm and 0.463 atm, respectively, what is the equilibrium partial pressure of Cl_2 at 250°C.





EXERCISE - 8

For the Haber process,



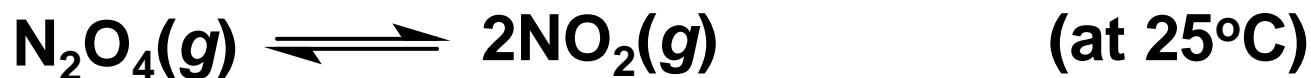
$$K_p = 1.45 \times 10^{-5} \text{ at } 500^\circ\text{C}.$$

In an equilibrium mixture of the three gases at 500°C , the partial pressure of H_2 is 0.928 atm and that of N_2 is 0.432 atm.

What is the partial pressure of NH_3 in this equilibrium?

Keep in mind!

The value of K_C and K_P depend on **how the equilibrium equation is written and balanced.**



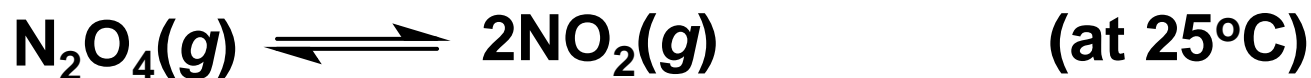
$$K_C = \frac{[\text{NO}_2]^2}{[\text{N}_2\text{O}_4]} = 4.63 \times 10^{-3}$$



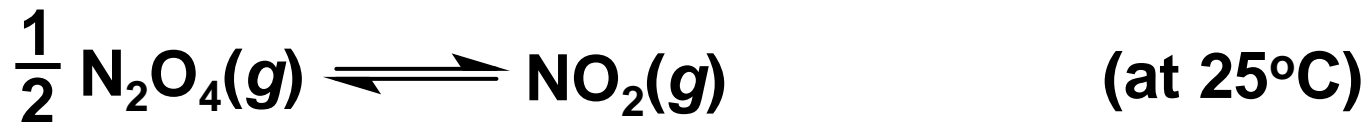
$$K_C = \frac{[\text{N}_2\text{O}_4]}{[\text{NO}_2]^2} = 216$$

Keep in mind!

The value of K_C and K_P depend on **how the equilibrium equation is written and balanced.**



$$K_C = \frac{[\text{NO}_2]^2}{[\text{N}_2\text{O}_4]} = 4.63 \times 10^{-3}$$



$$K_C = \frac{[\text{NO}_2]}{[\text{N}_2\text{O}_4]^{1/2}} = 0.0680$$

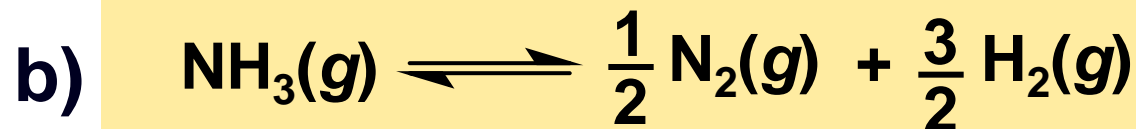
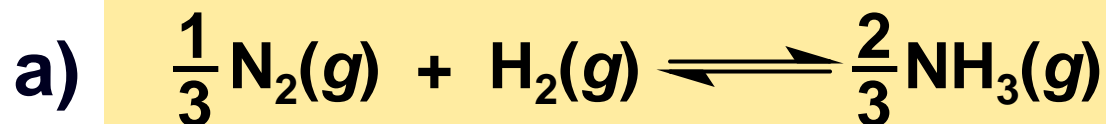


EXERCISE - 9

For the ammonia-formation reaction,



$K_C = 2.4 \times 10^{-3}$ at 1000 K. If we change the coefficients of this equation, what are the values of K_C for the following balanced equations?





EXERCISE - 10

At 25°C, $K_C = 7.0 \times 10^{25}$ for the reaction:



What is the value of K_C for the reaction:





HETEROGENEOUS EQUILIBRIUM

☞ Reactants and products are in **different phases**.



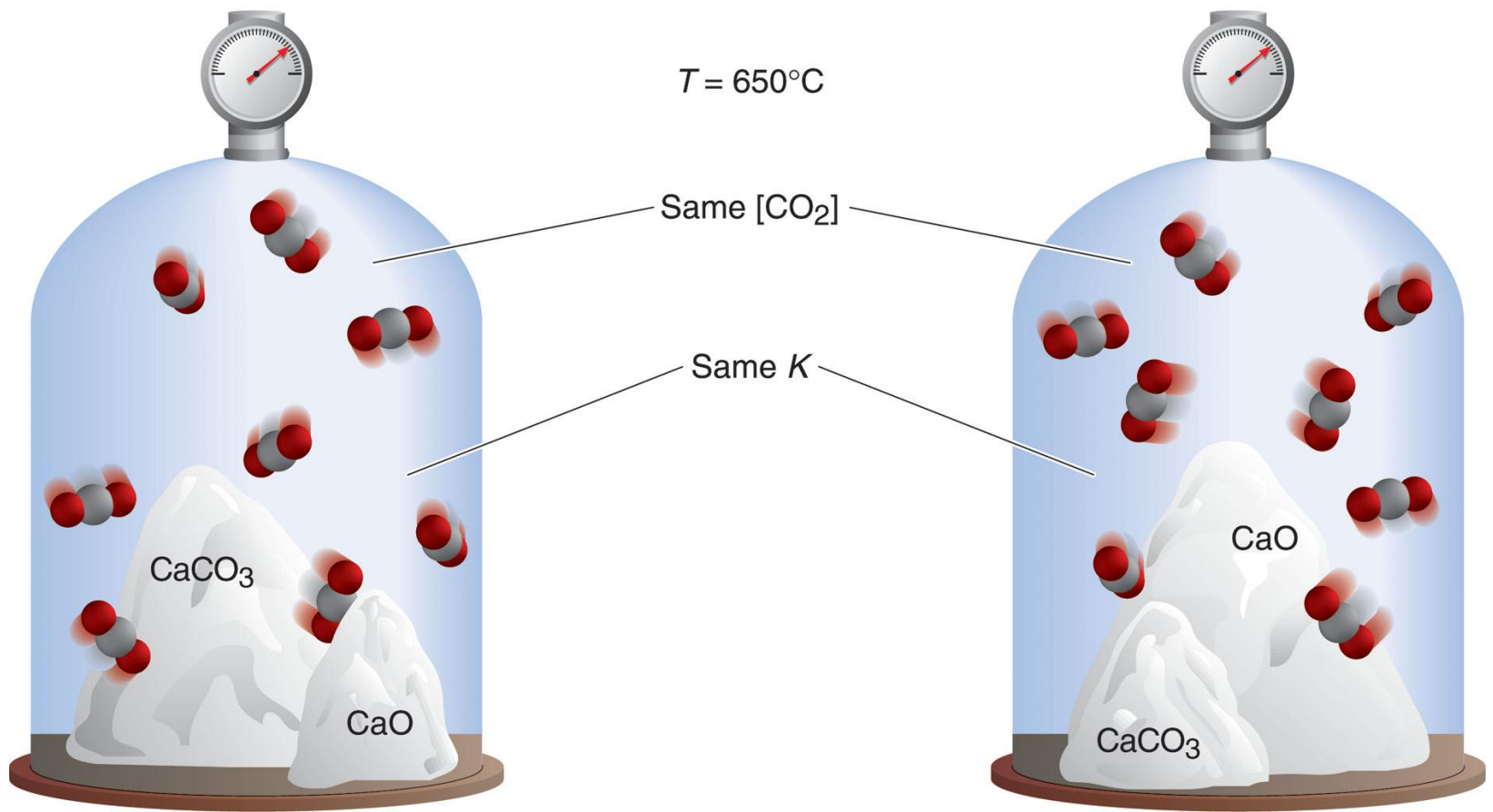
$$K'_c = \frac{[\text{CaO}][\text{CO}_2]}{[\text{CaCO}_3]}$$

$$[\text{CaCO}_3] = \text{constant}$$
$$[\text{CaO}] = \text{constant}$$

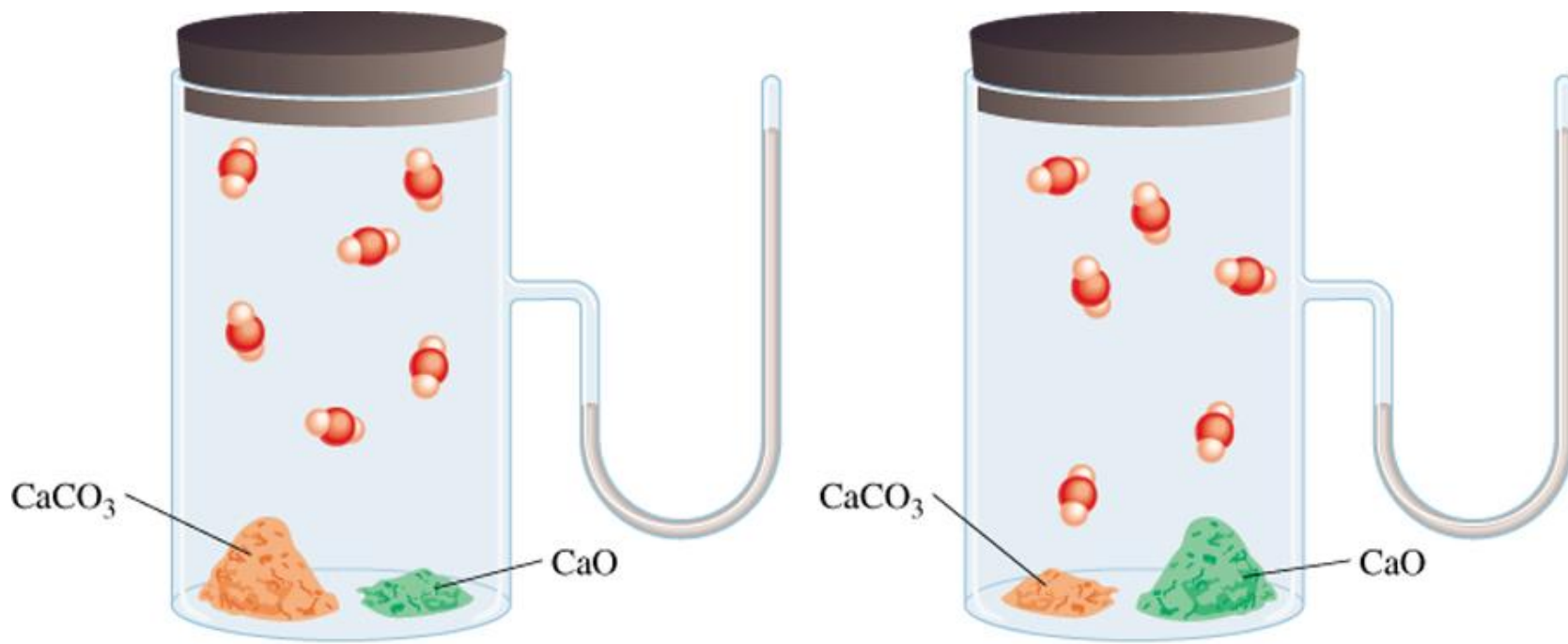
$$K_c = [\text{CO}_2]$$

$$K_p = P_{\text{CO}_2}$$

The concentration of **pure solids**, **pure liquids** and **solvents** do **not appear in the equilibrium constant expression**.



- ☞ A pure solid always has the **same concentration at a given temperature** → **same number of moles per liter of the solid.**
- ☞ Just as it has **same density at any given temperature.**
- ☞ Same reason applies to **pure liquid.**



$$P_{\text{CO}_2} = K_P$$

P_{CO_2} does not depend on the amount of CaCO_3 or CaO .



EXAMPLE - 3

ANS:

Write equilibrium constant expression for K_C and K_P for the formation of nickel tetracarbonyl, which is used to separate nickel from other impurities:



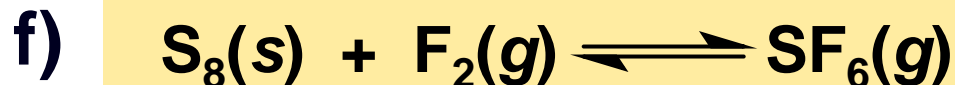
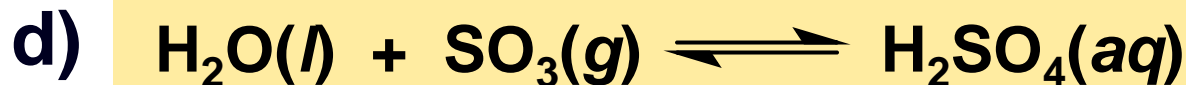
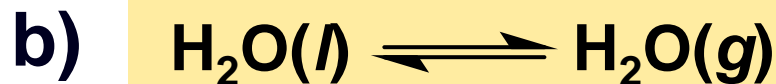
$$K_C = \frac{[\text{Ni}(\text{CO})_4]}{[\text{CO}]^4}$$

$$K_P = \frac{P_{\text{Ni}(\text{CO})_4}}{P_{\text{CO}}^4}$$



EXERCISE - 11

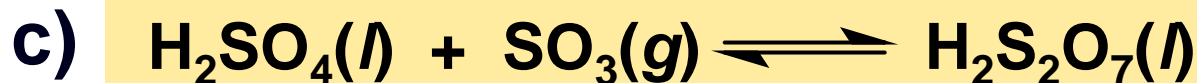
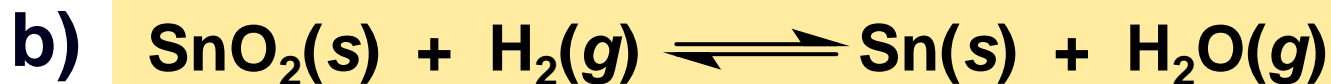
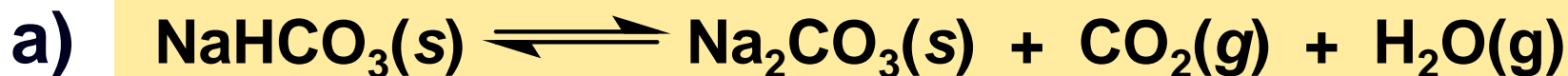
Balance each of the following equations and write its equilibrium constant expression, K_C and K_P :





EXERCISE - 12

Balance each of the following equations and write its equilibrium constant expression, K_C and K_P :





EXAMPLE - 4

ANS:

Consider the following equilibrium at 295 K:



The partial pressure of each gas is 0.265 atm.
Calculate K_p for the reaction?

$$K_p = P_{\text{NH}_3} P_{\text{H}_2\text{S}} = 0.265 \times 0.265 = 0.0702$$



EXERCISE - 13

At equilibrium in the following reaction at 60°C, the partial pressure of the gases are found to be $P_{\text{HI}} = 3.65 \times 10^{-3}$ atm and $P_{\text{H}_2\text{S}} = 0.996$ atm.

What is the value of K_p for the reaction?





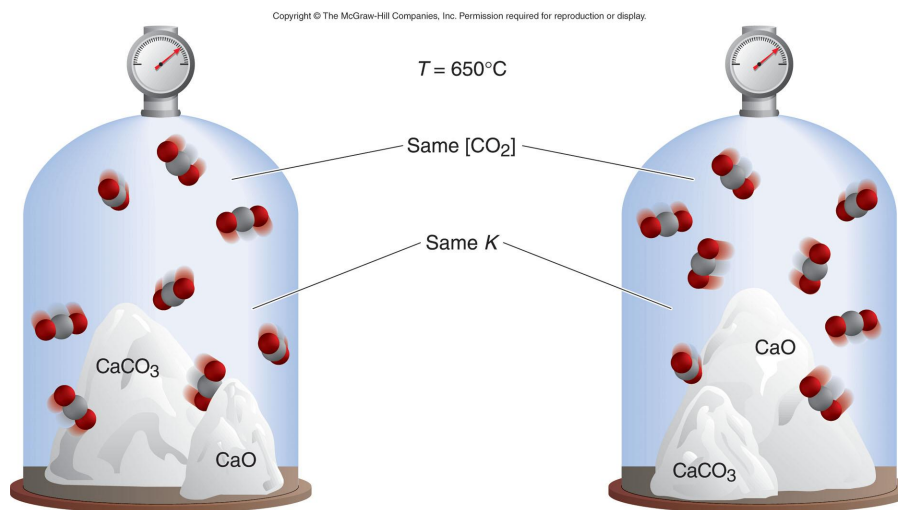
EXERCISE - 14

At equilibrium, the pressure of reacting mixture



is 0.105 atm at 350°C.

Calculate K_p for this reaction.

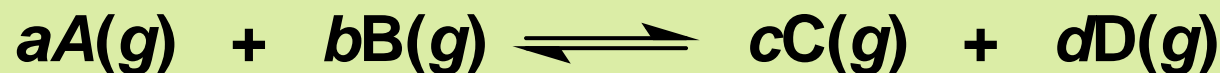




RELATION BETWEEN K_p AND K_c

In most cases

$$K_C \neq K_P$$



$$K_C = \frac{[C]^c [D]^d}{[A]^a [B]^b} \quad K_P = \frac{P_C^c P_D^d}{P_A^a P_B^b}$$

$$K_P = K_C (RT)^{\Delta n}$$

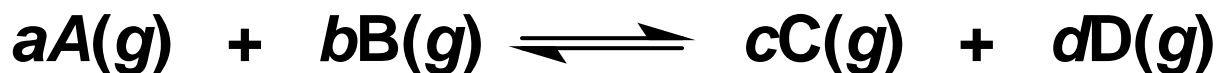
But, how do we derive this equation?

Δn = moles of gaseous products = $(c + d) - (a + b)$
– moles of gaseous reactants



Derivation of equation: $K_p = K_c(RT)^{\Delta n}$

Let us consider the following equilibrium in gas phase:



The equilibrium constant K_C :

$$K_C = \frac{[C]^c [D]^d}{[A]^a [B]^b}$$

The expression for K_P :

$$K_P = \frac{P_C^c P_D^d}{P_A^a P_B^b}$$

Assuming the gases behave as ideal gases:

$$PV = nRT$$

$$P_A = \frac{n_A RT}{V} \\ = [A]RT$$

$$P_B = \frac{n_B RT}{V} \\ = [B]RT$$

$$P_C = \frac{n_C RT}{V} \\ = [C]RT$$

$$P_D = \frac{n_D RT}{V} \\ = [D]RT$$



Derivation of equation: $K_p = K_c(RT)^{\Delta n}$

$$P_A = \frac{n_A}{V} RT \quad P_B = \frac{n_B}{V} RT \quad P_C = \frac{n_C}{V} RT \quad P_D = \frac{n_D}{V} RT$$
$$= [A]RT \quad = [B]RT \quad = [C]RT \quad = [D]RT$$

*Notice that, n_A/V , n_B/V , n_C/V and n_D/V have units mol L^{-1} and been replaced by $[A]$, $[B]$, $[C]$ and $[D]$

By substituting these relations into the expression of K_p :

$$K_p = \frac{P_C^c P_D^d}{P_A^a P_B^b}$$
$$= \frac{([C]RT)^c \times ([D]RT)^d}{([A]RT)^a \times ([B]RT)^b}$$
$$= \frac{[C]^c [D]^d}{[A]^a [B]^b} \times (RT)^{(c+d)-(a+b)}$$
$$= K_c(RT)^{\Delta n}$$

$\Delta n = \text{moles of gaseous products} - \text{moles of gaseous reactants}$

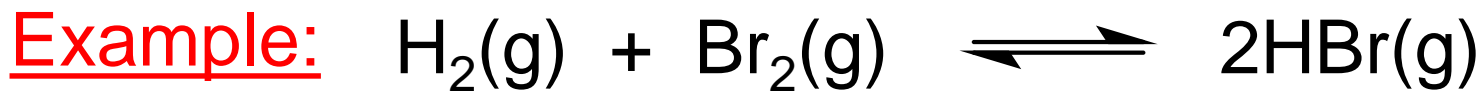
Keep in mind!

Relationship between K_p and K_c can also be written as $K_p = K_c(0.0821 T)^{\Delta n}$

$$R = 0.0821 \text{ L atm mol}^{-1} \text{ K}^{-1}$$

If $\Delta n = 0$: $K_p = K_c(0.0821 T)^0$

$$K_p = K_c$$



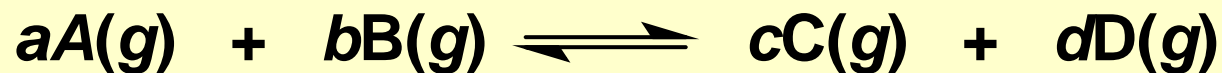


EXERCISE - 15

Show how you can get the following equation:

$$K_P = K_C(RT)^{\Delta n}$$

Hints:



$$K_C = \frac{[C]^c [D]^d}{[A]^a [B]^b} \quad K_P = \frac{P_C^c P_D^d}{P_A^a P_B^b}$$

$$PV = nRT$$



EXAMPLE - 5

ANS:

The equilibrium concentrations for the reaction between carbon monoxide and molecular chlorine to form $\text{COCl}_2 (g)$ at 74°C are $[\text{CO}] = 0.012 \text{ M}$, $[\text{Cl}_2] = 0.054 \text{ M}$, and $[\text{COCl}_2] = 0.14 \text{ M}$. Calculate the equilibrium constants K_C and K_P .



$$K_C = \frac{[\text{COCl}_2]}{[\text{CO}][\text{Cl}_2]} = \frac{0.14}{0.012 \times 0.054} = 216$$

$$K_P = K_C (RT)^{\Delta n}$$

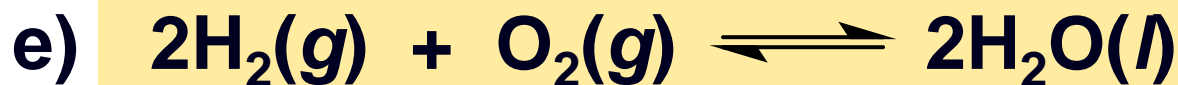
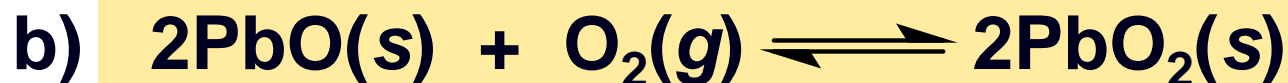
$$\Delta n = 1 - 2 = -1 \quad R = 0.0821 \quad T = 273 + 74 = 347 \text{ K}$$

$$K_P = 216 \times (0.0821 \times 347)^{-1} = 7.58$$



EXERCISE - 16

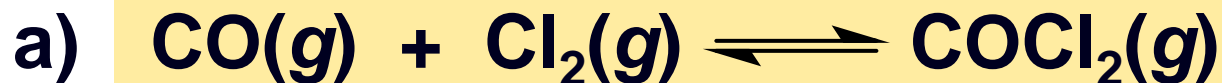
Determine Δn_{gas} for each of the following reactions:





EXERCISE - 17

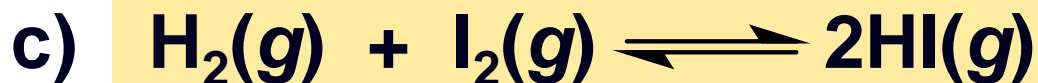
Calculate K_C for the following equilibria:



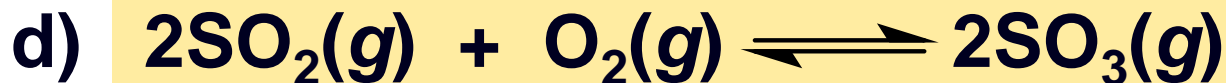
$$K_p = 3.9 \times 10^{-2} \text{ at } 1000\text{K}$$



$$K_p = 28.5 \text{ at } 500\text{K}$$



$$K_p = 49 \text{ at } 730\text{K}$$

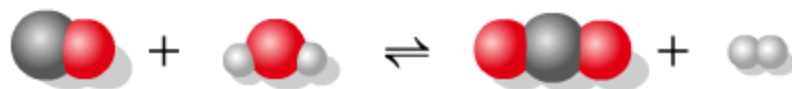
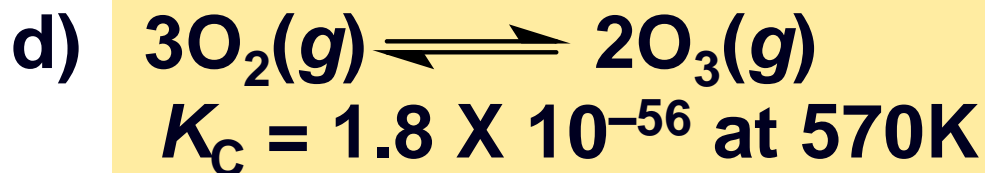
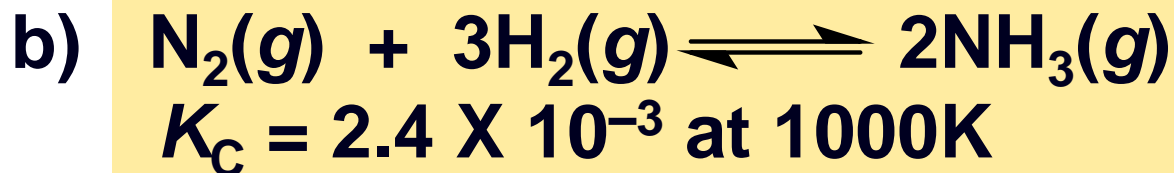
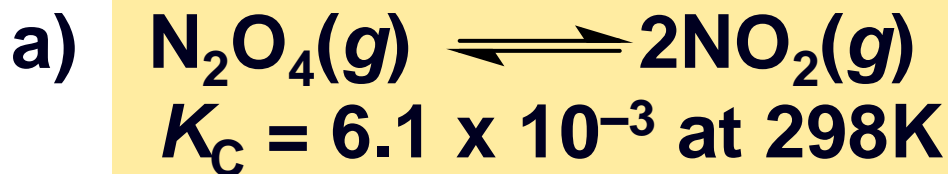


$$K_p = 2.5 \times 10^{10} \text{ at } 500\text{K}$$



EXERCISE - 18

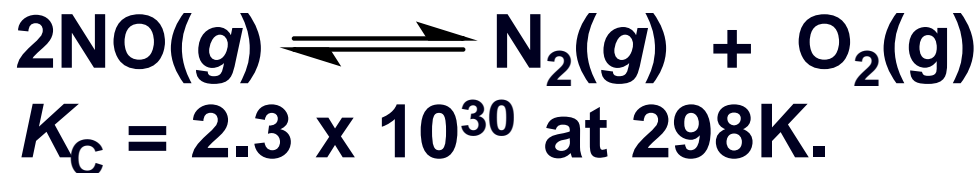
Calculate K_p for the following equilibria:





EXERCISE - 19

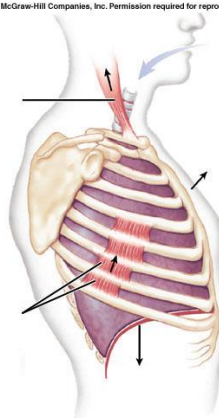
Nitric oxide, oxygen, and nitrogen react by the following equation:



In the atmosphere, $P_{\text{O}_2} = 0.209 \text{ atm}$ and $P_{\text{N}_2} = 0.781 \text{ atm}$.

What is the partial pressure of NO in the air we breath?

Inspiration





EXERCISE - 20

Consider the following heterogeneous equilibrium:



At 800°C, the pressure of CO_2 is 0.236 atm.

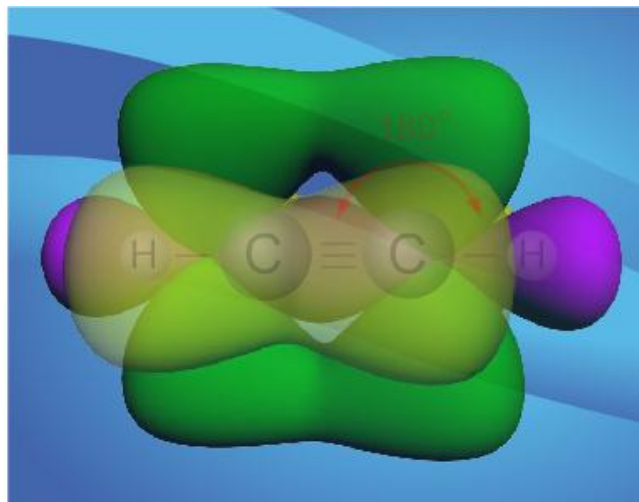
Calculate K_p and K_c for the reaction at this temperature.



EXERCISE - 21

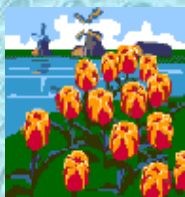
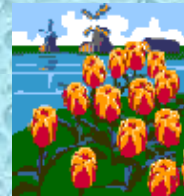
For which of the following reactions does $K_p = K_c$?

- a) $2\text{H}_2(g) + \text{C}_2\text{H}_2(g) \rightleftharpoons \text{C}_2\text{H}_6(g)$
b) $\text{N}_2(g) + \text{O}_2(g) \rightleftharpoons 2\text{NO}(g)$
c) $2\text{NO}(g) + \text{O}_2(g) \rightleftharpoons 2\text{NO}_2(g)$





*END OF
SLIDE SHOW*





CHEMICAL EQUILIBRIUM

6.2 Equilibrium Constants (Part II)

At the end of the lesson, students should be able to:

- (a) Calculate K_c , K_p or the quantities of species present at equilibrium.
- (b) Define and determine the degree of dissociation, α .

LESSON DURATION: 2 hours



EQUILIBRIUM PROBLEMS

Two types:

1

➡ **Equilibrium quantities** (concentrations , partial pressure) are given

➡ Solve for K_C or K_P

2

➡ **Initial quantities** (initial concentrations , initial partial pressure) and K_P or K_C are given

➡ Solve for **equilibrium quantities** (concentrations , partial pressure)



USING A REACTION (*ICE*) TABLE

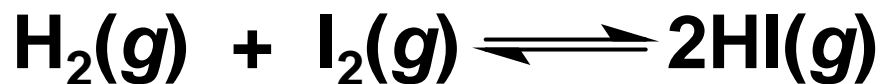
1. Express the **equilibrium concentrations** of all species in terms of the **initial concentrations** and a single **unknown x** , which represents the **change in concentration**.
2. Write the equilibrium constant expression in terms of the equilibrium concentrations. Knowing the value of the equilibrium constant, **solve for x** .
3. Having solved for x , calculate the **equilibrium concentrations** of all species.





EXAMPLE - 6

At a certain temperature, a mixture of H_2 and I_2 was prepared by placing 0.200 mol of H_2 and 0.200 mol of I_2 into a 2.00 L flask. After a period of time the equilibrium



was established.

At equilibrium, the concentration of I_2 concentration had dropped to 0.020 M. What is the value of K_C for this reaction at this temperature?





EXAMPLE - 6

ANS:

	$\text{H}_2(\text{g})$	+	$\text{I}_2(\text{g})$	\rightleftharpoons	$2\text{HI}(\text{g})$
Initial (M)	$\frac{0.200 \text{ mol}}{2.00 \text{ L}}$		$\frac{0.200 \text{ mol}}{2.00 \text{ L}}$		0.000
	= 0.100		= 0.100		
Change (M)	- x		- x		+ 2x
Equilibrium (M)	$0.100 - x$		$0.100 - x$		$0.000 + 2x$
			= 0.020		= 2x

ICE

$$\begin{aligned}\text{So, } x &= 0.100 - 0.020 \\ &= 0.080\end{aligned}$$

$$[\text{I}_2] = 0.020 \text{ M}$$

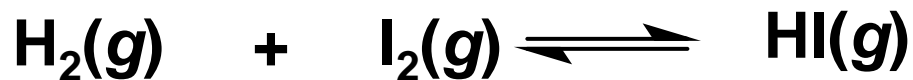
$$\begin{aligned}[\text{H}_2] &= (0.100 - 0.080) \text{ M} \\ &= 0.020 \text{ M}\end{aligned}$$

$$\begin{aligned}[\text{HI}] &= 2 \times 0.080 \text{ M} \\ &= 0.160 \text{ M}\end{aligned}$$



EXAMPLE - 6

ANS:



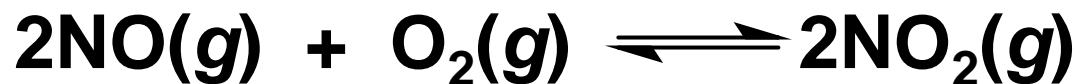
$$[\text{H}_2] = 0.020 \text{ M} \quad [\text{I}_2] = 0.020 \text{ M} \quad [2\text{HI}] = 0.160 \text{ M}$$

$$\begin{aligned} K_c &= \frac{[\text{HI}]^2}{[\text{H}_2] [\text{I}_2]} \\ &= \frac{(0.160)^2}{0.020 \times 0.020} \\ &= 64.0 \end{aligned}$$



EXAMPLE - 7

The atmospheric oxidation of nitric oxide,



was studied at 184°C with pressure of 1.000 atm of NO and 1.000 atm of O_2 .

At equilibrium, $P_{\text{O}_2} = 0.506$ atm.

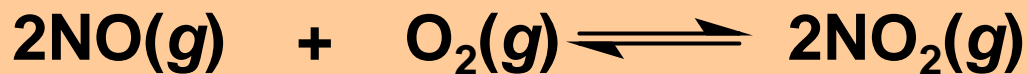
Calculate K_p .





EXAMPLE - 7

ANS:



Initial (atm)	1.000	1.000	0.000
Change (atm)	$-2x$	$-x$	$+2x$
Equilibrium (atm)	$1.000 - 2x$	$1.000 - x$ $= 0.506$	$0.000 + 2x$ $= 2x$

$$\text{So, } x = 1.000 - 0.506$$

$$= 0.494$$

$$P_{\text{NO}} = (1.000 - 2 \times 0.494) \text{ atm}$$
$$= 0.012 \text{ atm}$$

$$P_{\text{NO}_2} = 2 \times 0.494 \text{ atm}$$
$$= 0.988 \text{ atm}$$

$$P_{\text{O}_2} = 0.506 \text{ atm}$$



EXAMPLE - 7

ANS:



$$P_{\text{NO}} = 0.012 \text{ atm}$$

$$P_{\text{O}_2} = 0.506 \text{ atm}$$

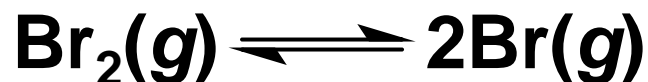
$$P_{\text{NO}_2} = 0.988 \text{ atm}$$

$$\begin{aligned} K_p &= \frac{P_{\text{NO}_2}^2}{P_{\text{NO}}^2 P_{\text{O}_2}} \\ &= \frac{(0.988)^2}{(0.012)^2 \times 0.506} \\ &= 1.34 \times 10^4 \end{aligned}$$



EXAMPLE - 8

At 1280°C the equilibrium constant (K_c) for the reaction



is 1.1×10^{-3} . If the initial concentrations are $[\text{Br}_2] = 0.063 \text{ M}$ and $[\text{Br}] = 0.012 \text{ M}$, calculate the concentrations of these species at equilibrium.

ANS:

Let x be the change in concentration of Br_2

	$\text{Br}_2(g)$	\rightleftharpoons	$2\text{Br}(g)$
Initial (M)	0.063		0.012
Change (M)	$-x$		$+2x$
Equilibrium (M)	$0.063 - x$		$0.012 + 2x$



EXAMPLE - 8

ANS:

	$\text{Br}_2(\text{g})$	\rightleftharpoons	$2\text{Br}(\text{g})$
Initial (M)	0.063		0.012
Change (M)	$-x$		$+2x$
Equilibrium (M)	$0.063 - x$		$0.012 + 2x$

$$K_c = \frac{[\text{Br}]^2}{[\text{Br}_2]} \quad K_c = \frac{(0.012 + 2x)^2}{0.063 - x} = 1.1 \times 10^{-3}$$

 Solve for x



EXAMPLE - 8

ANS:

Initial (M)	0.063	0.012
Change (M)	- x	+ 2x
Equilibrium (M)	0.063 - x	0.012 + 2x

$$K_c = \frac{(0.012 + 2x)^2}{0.063 - x} = 1.1 \times 10^{-3} \quad \leftarrow \text{given}$$

$$4x^2 + 0.048x + 0.000144 = 0.0000693 - 0.0011x$$

$$4x^2 + 0.0491x + 0.0000747 = 0$$

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = -0.0105$$

$$x = -0.00178$$



EXAMPLE - 8

ANS:

👉 Determine **chemically meaningful x value**

	$\text{Br}_2(\text{g}) \rightleftharpoons 2\text{Br}(\text{g})$	
Initial (M)	0.063	0.012
Change (M)	- x	+ 2x
Equilibrium (M)	$0.063 - x$	$0.012 + 2x$
(x = - 0.0105)	= 0.0705	= - 0.009
(x = - 0.00178)	= 0.0648	= 0.00844

WRONG
WAY

correct

Note: Only **one x value makes sense chemically!**

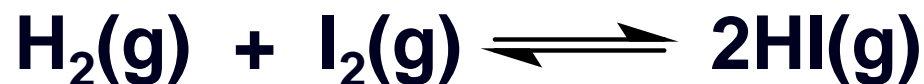
At equilibrium, $[\text{Br}] = 0.00844 \text{ M}$

$[\text{Br}_2] = 0.0648 \text{ M}$



EXERCISE - 22

At particular temperature, suppose that the initial concentrations of H_2 , I_2 , and HI are 0.00623 M, 0.00414 M and 0.0224 M.

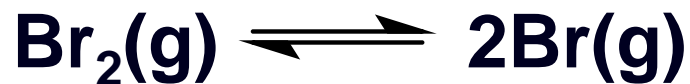


Calculate the concentrations of these species ($[\text{H}_2]$, $[\text{I}_2]$, $[\text{HI}]$) at equilibrium.



EXERCISE - 23

At 1280°C the equilibrium constant (K_C) for the reaction



is 1.1×10^{-3} . If the initial concentrations are $[\text{Br}_2] = 6.3 \times 10^{-2} \text{ M}$ and $[\text{Br}] = 1.2 \times 10^{-2} \text{ M}$.

Calculate the concentrations of these species at equilibrium.





EXERCISE - 24

Consider the following equilibrium process at 686°C:



The equilibrium concentrations of the reacting species are $[\text{CO}] = 0.050 \text{ M}$, $[\text{H}_2] = 0.045 \text{ M}$, $[\text{CO}_2] = 0.086 \text{ M}$, and $[\text{H}_2\text{O}] = 0.040 \text{ M}$.

- Calculate K_C for the reaction at 686°C.
- If we add CO_2 to increase its concentration to 0.50 M, what will be the concentrations of all gases be when equilibrium is reestablished?



EXERCISE - 25

In a particular experiment, it was found that when $\text{O}_2(\text{g})$ and $\text{CO}(\text{g})$ were mixed and reacted according to the equation



The O_2 concentration decreased by 0.030 M when the reaction reached equilibrium. How had the concentrations of CO and CO_2 changed?



EXERCISE - 26

The reaction



has $K_C = 4.06$ at 500°C . If 0.100 mol of CO and 0.100 mol of $\text{H}_2\text{O}(g)$ are placed in a 1.00 liter reaction vessel at this temperature, what are the concentration of the reactants and products when the system reaches equilibrium?





EXERCISE - 27

The reaction



has $K_c = 4.06$ at 500°C .

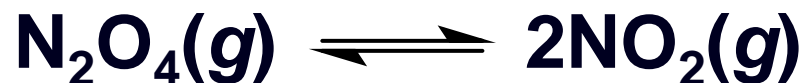
Suppose 0.0600 mol each of CO and H₂O are mixed with 0.100 mol each of CO₂ and H₂ in a 1.00 L reaction vessel.

What will the concentrations of all the substances be when the mixture reaches equilibrium at this temperature?

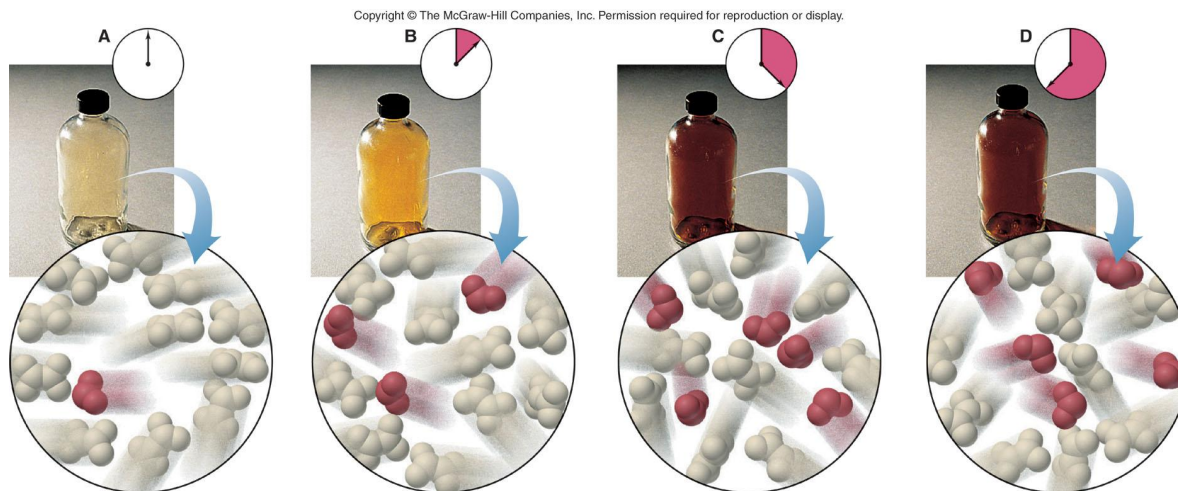


EXERCISE - 28

At a certain temperature $K_C = 4.50$ for the reaction



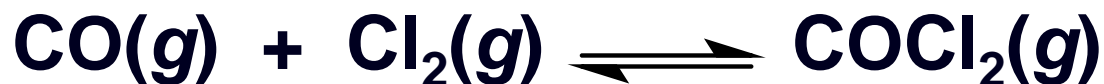
If 0.300 mol of N_2O_4 is placed into a 2.00 L container at this temperature, what will be the equilibrium concentrations of both gases?





EXERCISE - 29

Phosgene (COCl_2) is toxic substance that forms readily from carbon monoxide and chlorine at elevated temperatures:



If 0.350 mol of each reactant is placed a 0.500-L flask at 600 K, what are the concentrations of each substance at equilibrium?

($K_C = 4.95$ at this temperature)



Vocabulary: *elevated*
increasing, high



EXERCISE - 30

Fuel engineers use the extent of the change from CO and H₂O to CO₂ and H₂ to regulate the proportions of synthetic fuel mixture.



If 0.250 mol of CO and 0.250 mol of H₂O are placed in a 125-mL flask at 900 K, what is the equilibrium concentrations of each gas in the mixture?

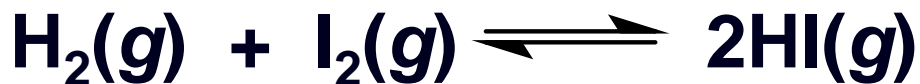
At 900 K, $K_C = 1.56$.





EXERCISE - 31

A 1.000-L flask is filled with 1.000 mol of H_2 and 2.000 mol of I_2 at 448°C .



$$K_{\text{C}} = 50.5 \text{ at } 448^\circ\text{C}.$$

What is the partial pressure of H_2 , I_2 and HI at equilibrium?



EXERCISE - 32

Hydrogen iodide decomposes according to the reaction



A sealed 1.50-L container initially holds 0.00623 mol of H_2 , 0.00414 mol of I_2 , and 0.0244 mol of HI at 703 K.

When equilibrium is reached, the concentration of $\text{H}_2(\text{g})$ is 0.00467 M.

What are the equilibrium concentrations of $\text{HI}(\text{g})$ and $\text{I}_2(\text{g})$?



EXERCISE - 33

Compound A decomposes according to the equation



A sealed 1.50-L reaction vessel initially contains 1.75×10^{-3} mol of A(g), 1.25×10^{-3} mol of B(g), and 6.50×10^{-4} mol of C(g) at 100°C .

When equilibrium is reached, the concentration of A(g) is 2.15×10^{-3} M.

What are the equilibrium concentrations of B(g) and C(g) ?

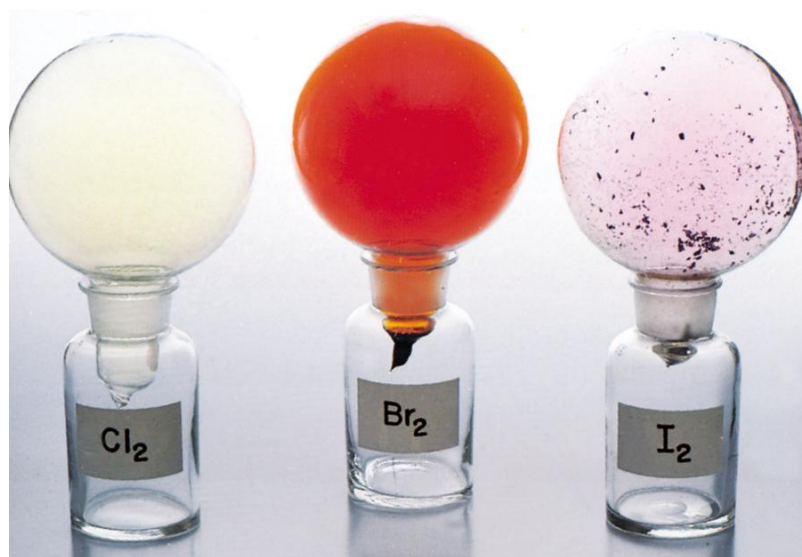


EXERCISE - 34

0.500 mol of ICl was placed in a 5.00-L flask and allowed to decompose at a high temperature:



Calculate the equilibrium concentrations of I₂, Cl₂, and ICl. ($K_C = 0.110$ at this temperature)





EXERCISE - 35

A United Nations toxicologist studying the properties of mustard gas, $\text{S}(\text{CH}_2\text{CH}_2\text{Cl})_2$, a blistering agent used in warfare, prepares a mixture of 0.675 M SCl_2 and 0.973 M C_2H_4 and allows to react at room temperature (20.0°C):



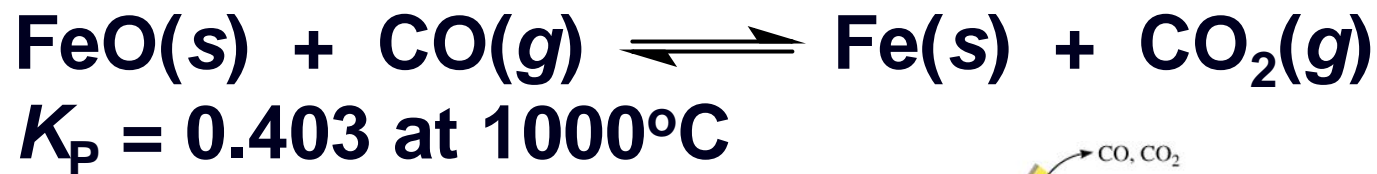
At equilibrium, $[\text{S}(\text{CH}_2\text{CH}_2\text{Cl})_2] = 0.350 \text{ M}$.
Calculate K_p .



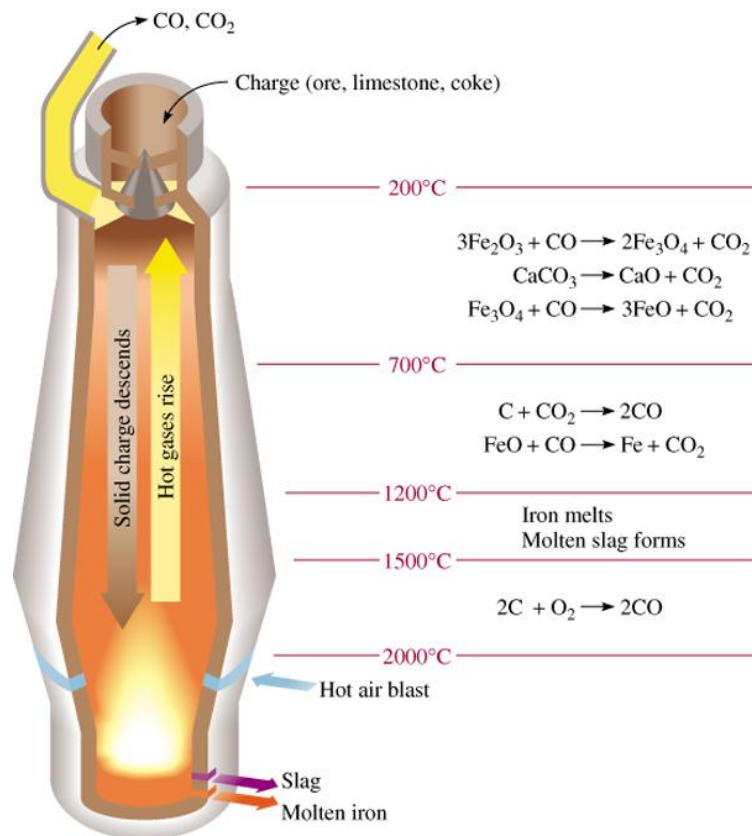


EXERCISE - 36

A key step in extraction of iron from its ore is



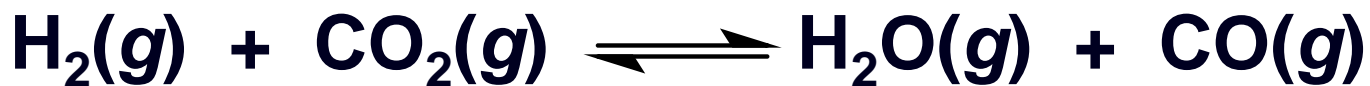
What are the equilibrium partial pressure of CO(g) and $\text{CO}_2\text{(g)}$ when 1.00 atm of CO(g) and excess FeO(s) react in a sealed container at 1000°C ?





EXERCISE - 37

An industrial chemist introduces 2.0 atm of H_2 and 2.0 atm of CO_2 into a 1.00-L container at 25°C and then raises the temperature to 700°C , at which $K_c = 0.534$:



How many grams of H_2 are present after equilibrium is established?





EXERCISE - 38

A quality control engineer examining the conversion of SO_2 to SO_3 in the manufacture of sulfuric acid determines that $K_C = 1.7 \times 10^8$ at 600K for the reaction



- a) At equilibrium $P_{\text{SO}_3} = 300$ atm and $P_{\text{O}_2} = 100$ atm. Calculate P_{SO_2} .
- b) The engineer places a mixture of 0.0040 mol of $\text{SO}_2(g)$ and 0.0028 mol of $\text{O}_2(g)$ in a 1.0-L container and raises the temperature to 1000K. At equilibrium, 0.0020 mol of $\text{SO}_3(g)$ is present. Calculate K_C and P_{SO_2} for this reaction at 1000K.



EQUILIBRIUM CALCULATIONS WHEN K_c IS VERY SMALL

👉 The **concentration change (x)** can often be **neglected**.

$$[A]_{\text{initial}} - x = [A]_{\text{equilibrium}} \approx [A]_{\text{initial}}$$

Note: You must **check** that the **assumption** is **justified** or not.

CHECK:
5% rule

$$\frac{x}{[A]_{\text{initial}}} \times 100 < 5\%$$

👉 Assumption is **OK**

$$\frac{x}{[A]_{\text{initial}}} \times 100 > 5\%$$

👉 Assumption is **NOT OK**

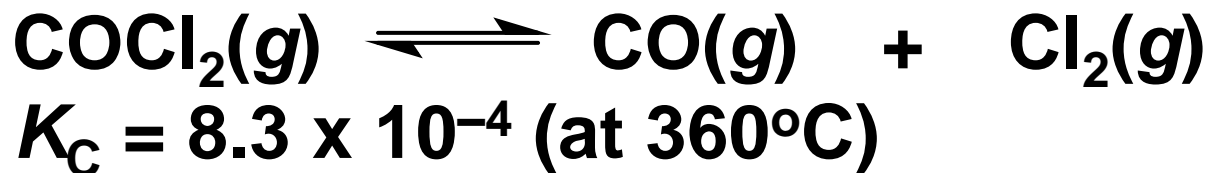
👉 Use **quadratic formula**



EXAMPLE - 9

ANS:

Phosgene is a potent chemical warfare agent that is now outlawed by international agreement. It decomposes by the reaction



Calculate $[\text{CO}]$, $[\text{Cl}_2]$, and $[\text{COCl}_2]$, when the following amounts of phosgene decompose and reach equilibrium in a 10-L flask:

- a) 5.000 mol of COCl_2
- b) 0.100 mol of COCl_2





EXAMPLE - 9

ANS:

a)

	$\text{COCl}_2(g)$	\rightleftharpoons	$\text{CO}(g)$	+	$\text{Cl}_2(g)$
Initial (M)	$\frac{5.000 \text{ mol}}{10.0 \text{ L}}$		0.000		0.000
	$= 0.500$				
Change (M)	$-x$		$+x$		$+x$
Equilibrium (M)	$0.500 - x$		x		x

$$K_c = \frac{[\text{CO}][\text{Cl}_2]}{[\text{COCl}_2]}$$

$$K_c = \frac{x^2}{(0.500 - x)} = 8.3 \times 10^{-4}$$

 Solve for x



EXAMPLE - 9

ANS:

$$K_c = \frac{[\text{CO}][\text{Cl}_2]}{[\text{COCl}_2]}$$

$$K_c = \frac{x^2}{(0.500 - x)} = 8.3 \times 10^{-4}$$

👉 Solve for x

K_c is very small

Assume x very small, $0.500 - x \approx 0.500$

$$K_c = \frac{x^2}{0.500} = 8.3 \times 10^{-4}$$

$$x^2 = 8.3 \times 10^{-4} \times 0.500$$

$$x = 2.0 \times 10^{-2}$$

Checking the assumption:

$$\frac{2.0 \times 10^{-2}}{0.500} \times 100 = 4 \% (< 5\%)$$

OK!



EXAMPLE - 9

ANS:

	$\text{COCl}_2(\text{g})$	\rightleftharpoons	$\text{CO}(\text{g})$	+	$\text{Cl}_2(\text{g})$
Initial (M)	= 0.500		0.000		0.000
Change (M)	- x		+ x		+ x
Equilibrium (M)	0.500 - x		x		x

$$(x = 2.0 \times 10^{-2})$$

$$[\text{CO}] = 2.0 \times 10^{-2} \text{ M}$$

$$[\text{Cl}_2] = 2.0 \times 10^{-2} \text{ M}$$

$$\begin{aligned} [\text{COCl}_2] &= (0.500 - 2.0 \times 10^{-2}) \text{ M} \\ &= 0.480 \text{ M} \end{aligned}$$



EXAMPLE - 9

ANS:

b)



Initial (M)	$\frac{0.100 \text{ mol}}{10.0 \text{ L}}$ $= 0.010$	0.000	0.000
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Change (M)	$-x$	$+x$	$+x$
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Equilibrium (M)	$0.010 - x$	x	x
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$$K_c = \frac{[\text{CO}][\text{Cl}_2]}{[\text{COCl}_2]}$$

$$K_c = \frac{x^2}{(0.010 - x)} = 8.3 \times 10^{-4}$$

 Solve for x



EXAMPLE - 9

ANS:

$$K_c = \frac{[\text{CO}][\text{Cl}_2]}{[\text{COCl}_2]}$$

$$K_c = \frac{x^2}{(0.010 - x)} = 8.3 \times 10^{-4}$$

👉 Solve for x

K_c is very small

Assume x very small, $0.010 - x \approx 0.010$

$$K_c = \frac{x^2}{0.010} = 8.3 \times 10^{-4}$$

$$x^2 = 8.3 \times 10^{-4} \times 0.010$$

$$x = 2.9 \times 10^{-3}$$

Checking the assumption:

$$\frac{2.9 \times 10^{-3}}{0.010} \times 100 = 29 \% (> 5\%)$$

NOT OK!



EXAMPLE - 9

ANS:

$$K_c = \frac{[\text{CO}][\text{Cl}_2]}{[\text{COCl}_2]} \quad K_c = \frac{x^2}{(0.010 - x)} = 8.3 \times 10^{-4}$$

👉 Solve for x using **quadratic formula**

$$x^2 + (8.3 \times 10^{-4})x - 8.3 \times 10^{-6} = 0$$

Do it yourself

$x = 2.5 \times 10^{-3}$ (the only **meaningful value of x**)

$$[\text{CO}] = 2.5 \times 10^{-3} \text{ M}$$

$$[\text{Cl}_2] = 2.5 \times 10^{-3} \text{ M}$$

$$[\text{COCl}_2] = (0.010 - 2.5 \times 10^{-3}) \text{ M}$$

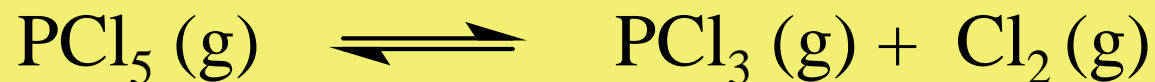
$$= 7.5 \times 10^{-3} \text{ M}$$



DEGREE OF DISSOCIATION, α

Dissociation reaction: a molecule is broken down into smaller molecules, atoms or ions

EXAMPLE:



Fraction or the percentage of molecules that dissociate is called **degree of dissociation, α**

$\alpha = 1$ or **100%** if **complete dissociation occurs**

If **incomplete dissociation occurs**:

$$\alpha = \frac{[\]_{\text{changes}}}{[\]_{\text{initial}}} \times 100\%$$



THERMAL DISSOCIATION

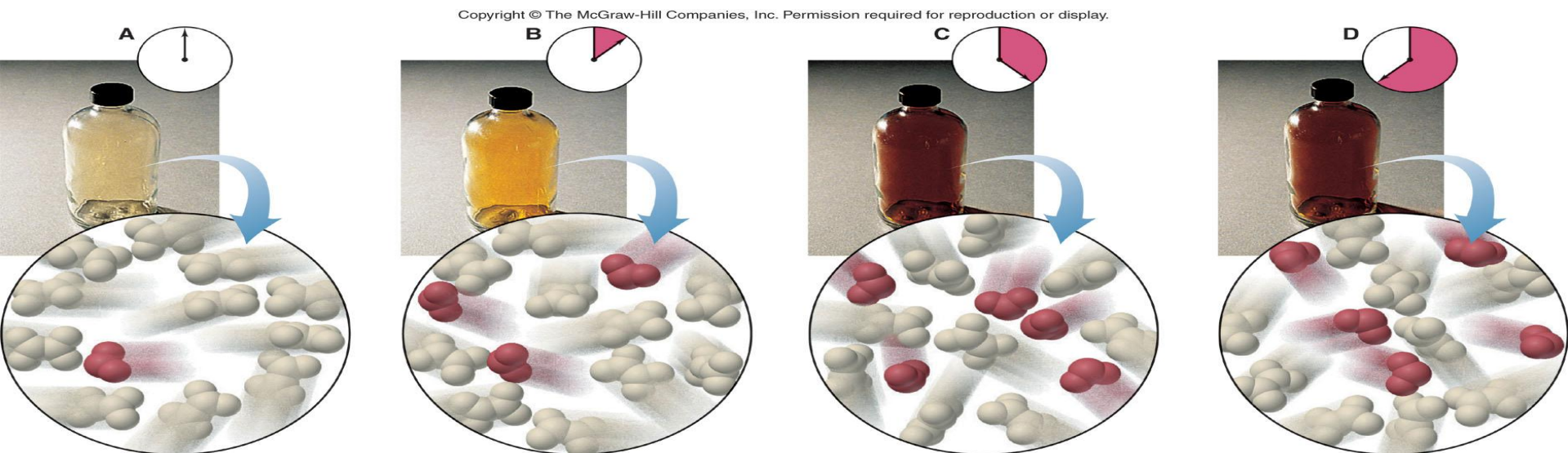
- A **reversible reaction** brought about by the **application of heat**
- When **cool**, the **products bond again to give the original compound**
- Example: PCl_5 , N_2O_4 and NH_4Cl





EXAMPLE - 10

The degree of dissociation of dinitrogen tetroxide at 250°C and 1 atm is 0.15.
Calculate the degree of dissociation at 250°C and 5 atm.





EXAMPLE - 10

ANS:

According to Dalton's law of partial pressure:

Partial pressure of $\text{NO}_2 = 0.3/1.15 \times 1\text{atm} = 0.261 \text{ atm}$

Partial pressure of $\text{N}_2\text{O}_4 = 0.85/1.15 \times 1\text{atm} = 0.739 \text{ atm}$

$$K_p = \frac{P_{\text{NO}_2}^2}{P_{\text{N}_2\text{O}_4}}$$

$$K_p = \frac{0.261^2}{0.739}$$

$$= 9.21 \times 10^{-2} \text{ atm}$$



EXAMPLE - 10

ANS:



Initial (mol)	1	0
Changes	-0.15	+0.15
Equilibrium (mol)	$1 - 0.15 = 0.85$	$2(0.15) = 0.30$

Total number of moles after dissociation

$$= 0.85 + 0.30$$

$$= 1.15 \text{ mol}$$



EXAMPLE - 10

ANS:

Let the degree of dissociation, α at 5 atm = x



Initial (mol)	1	0
Changes	- x	+ x
Equilibrium (mol)	$1 - x$	$2x$



EXAMPLE - 10

ANS:

$$P_{\text{NO}_2} = \frac{2x}{1 - x + 2x} \quad (5 \text{ atm})$$

$$P_{\text{N}_2\text{O}_4} = \frac{1x}{1 - x + 2x} \quad (5 \text{ atm})$$

$$K_p = \frac{(2x / 1 + x)^2 (5^2)}{(1 - x / 1 + x) (5)} = 9.21 \times 10^{-2}$$

$$x = 0.068$$

Only 6.8% of dinitrogen tetroxide dissociates at 250°C and 5 atm



EXERCISE - 39

6.2

At a pressure of 4.4×10^5 Pa and a temperature of $150\text{ }^\circ\text{C}$, phosphorus pentachloride is 25% dissociated. Calculate the partial pressure equilibrium constant for this reaction.



EXERCISE - 40

6.2

Hydrogen, a potential fuel, is found in great abundance in water. Before hydrogen can be used as a fuel, however, it must be separated from oxygen; the water must be split into H_2 and O_2 . one possibility is thermal decomposition, but this requires very high temperatures. Even at 1000°C , $K_C = 7.3 \times 10^{-18}$ for the reaction



If at 1000°C the H_2O concentration in a reaction vessel is set initially at 0.100 M , what will be the equilibrium concentration of H_2 ?

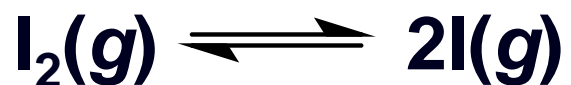




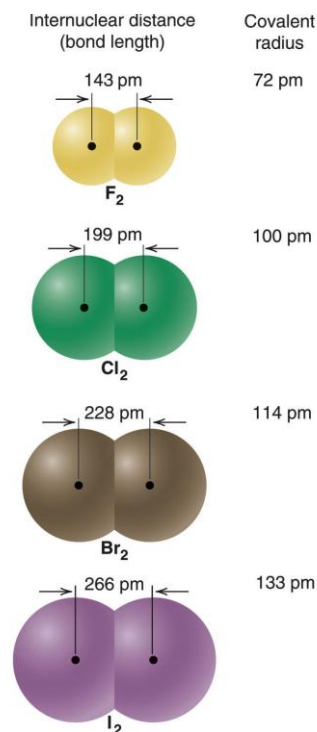
EXERCISE - 41

6.2

In a study of halogen bond strengths, 0.50 mol of I_2 was heated in a 2.5-L vessel, and the following reaction occurred:



- a) Calculate $[I_2]$ and $[I]$ at equilibrium at 600K; $K_C = 2.94 \times 10^{-10}$
- b) Calculate $[I_2]$ and $[I]$ at equilibrium at 2000K; $K_C = 0.209$

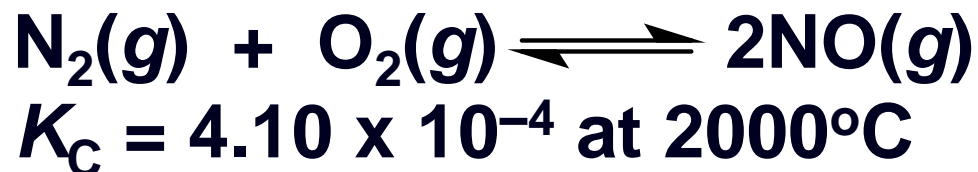




EXERCISE - 42

6.2

Even at high temperature, the formation of nitric oxide is not favored:



What is the equilibrium concentration of $\text{NO}(\text{g})$ when a mixture of 0.20 mol of $\text{N}_2(\text{g})$ and 0.15 mol of $\text{O}_2(\text{g})$ is allowed to come to equilibrium in a 1.0-L container at this temperature?



EXERCISE - 43

6.2

Nitrogen dioxide decomposes according to the reaction:



where $K_p = 4.48 \times 10^{-13}$ at a certain temperature.

A pressure of 0.75 atm of NO_2 is introduced into a container and allowed to come to equilibrium.

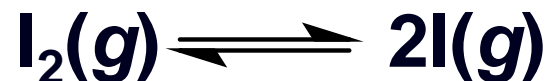
What are the equilibrium partial pressures of $\text{NO}(g)$ and $\text{O}_2(g)$?



EXERCISE - 44

6.2

The dissociation of molecular iodine into iodine atoms represented as



At 1000K, K_C for the reaction is 3.80×10^{-5} .

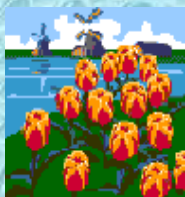
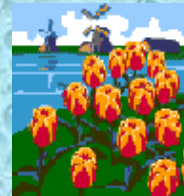
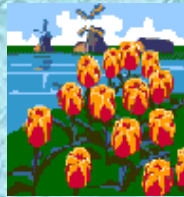
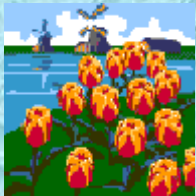
Suppose you start with 0.0456 mol of I_2 in a 2.30-L flask at 1000K.

What are the concentrations of the gases at equilibrium?





*END OF
SLIDE SHOW*





CHEMICAL EQUILIBRIUM

6.2 Equilibrium Constants (Part III)

At the end of the lesson, students should be able to:

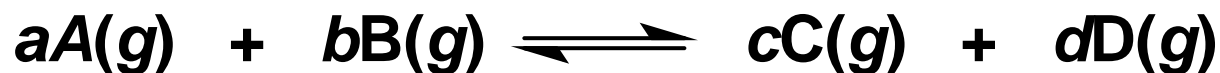
Deduce the expression for reaction quotient, Q and predict the direction of net reaction by comparing the values of Q and K_{eq} .

LESSON DURATION: 1 hour



REACTION QUOTIENT (Q)

- 👉 Calculated by substituting the **initial concentrations** (or **pressures**) of the reactants and products into K_C or K_P expression.



$$K_C = \frac{[C]^c [D]^d}{[A]^a [B]^b}$$

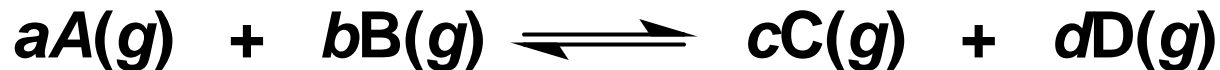
[A], [B], [C], [D] :
equilibrium
concentrations

$$Q_C = \frac{[C]^c [D]^d}{[A]^a [B]^b}$$

[A], [B], [C], [D] :
any (initial)
concentrations



COMPARING Q AND K



Suppose you know the value of K_C at any given temperature of the reaction.



How do you know if the **reaction has reached equilibrium**?

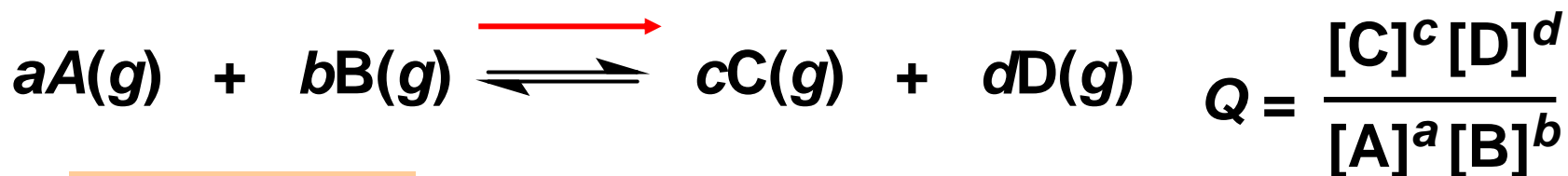


If it hasn't, how do you know in which **direction it is progressing to reach equilibrium**?

👉 Compare the value of K_C and Q_C .



COMPARING Q AND K



■ $Q < K$

👉 **Denominator** (reactants) is **large** relative to **numerator** (products)

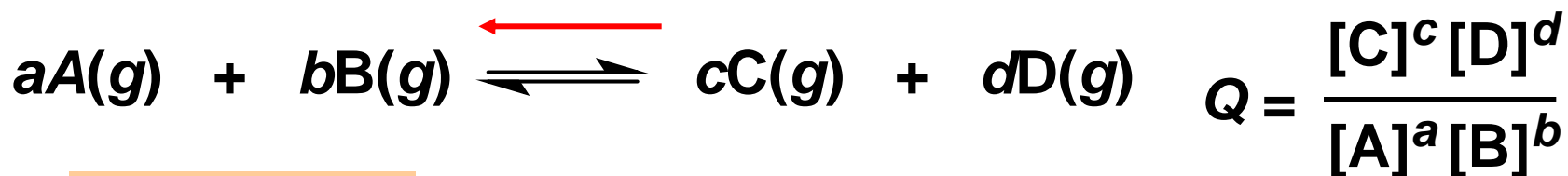
👉 To reach **equilibrium**, $Q = K$:
the **products must increase**, reactants decrease.

If $Q < K$, reactants \longrightarrow products

The reaction will **progress to the right** (more product forms) **until equilibrium is reached**.



COMPARING Q AND K



■ $Q > K$

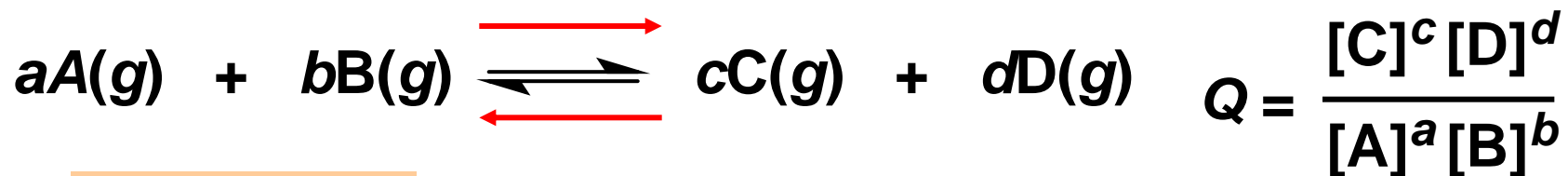
- 👉 **Denominator** (reactants) is **small** relative to **numerator** (products)
- 👉 To reach **equilibrium**, $Q = K$:
the **products must decrease**, reactants increase.

If $Q > K$, reactants \longleftarrow products

The reaction will **progress to the left** (more reactant forms) **until equilibrium is reached**.



COMPARING Q AND K

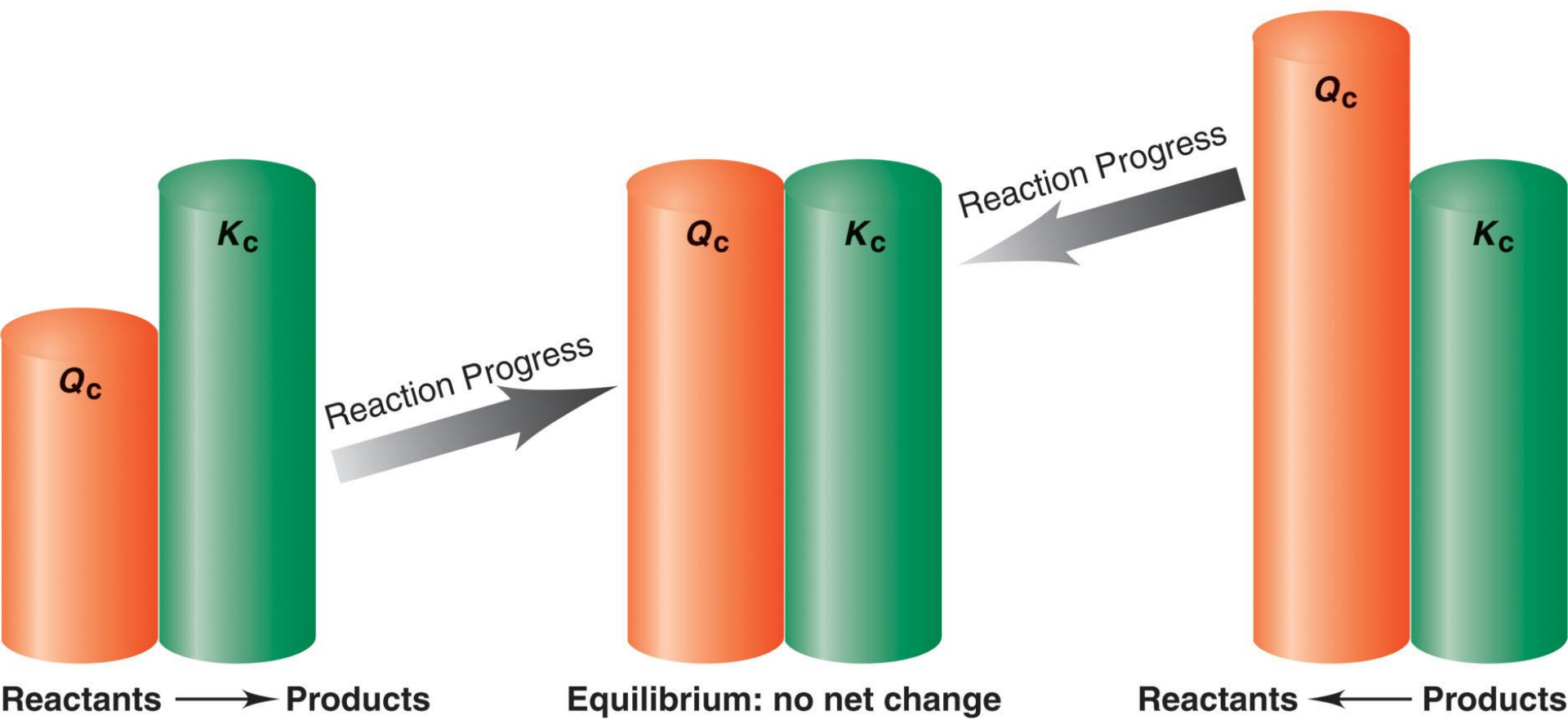


$$\blacksquare \quad Q = K$$

👉 When the reactant and product concentrations (or pressures) has **attained** their **equilibrium** values.

If $Q = K$, reactants \rightleftharpoons products

No further net change.

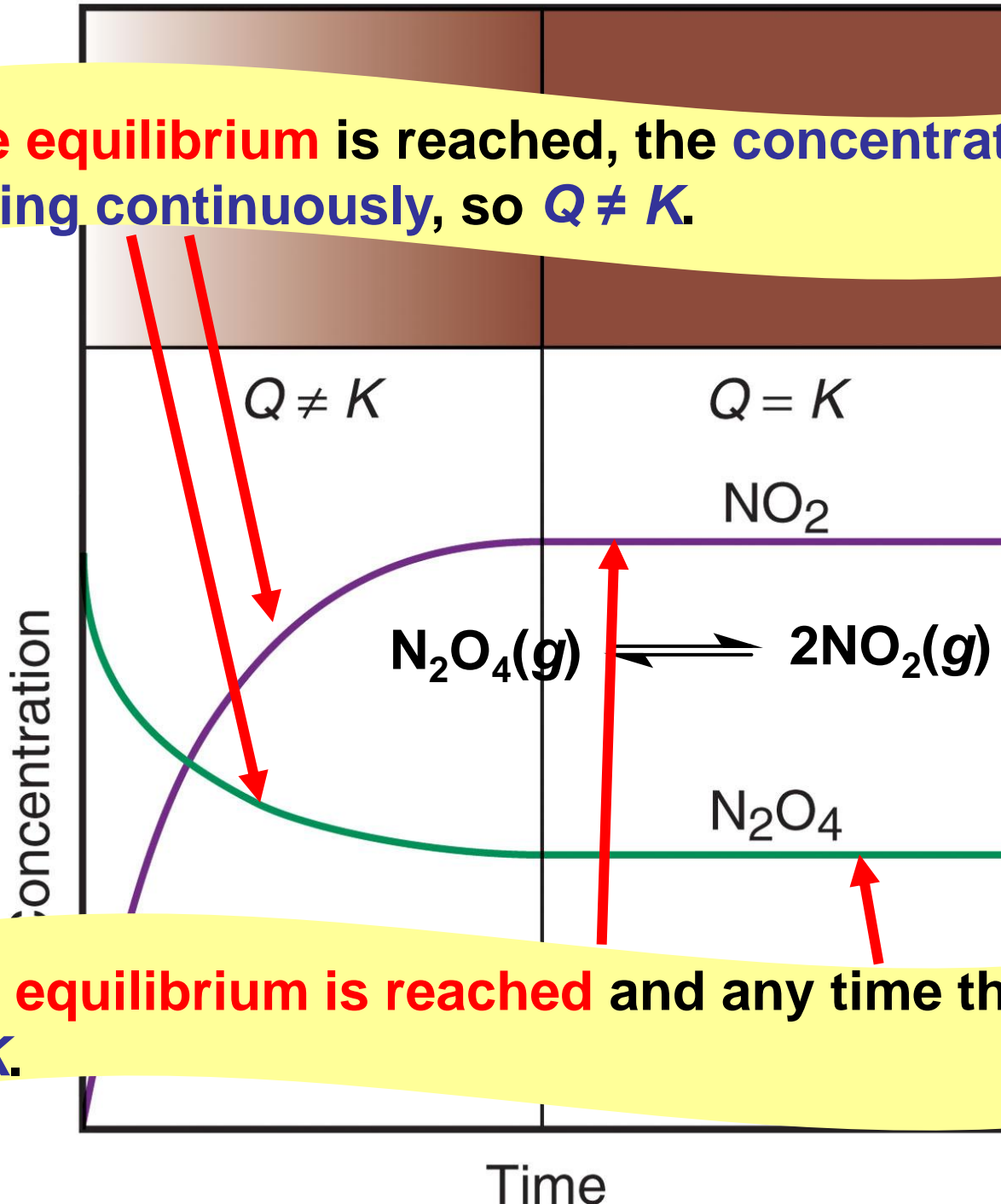


$Q < K$

$Q = K$

$Q > K$

Before equilibrium is reached, the concentration are changing continuously, so $Q \neq K$.



Once equilibrium is reached and any time thereafter, $Q = K$.



EXAMPLE - 11

K_C for the formation of nitrosyl chloride, an orange–yellow compound, from nitric oxide and molecular chlorine



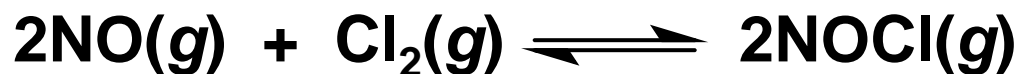
is 6.5×10^4 at 35°C . In certain experiment, 2.0×10^{-2} mole of NO, 8.3×10^{-3} mole of Cl_2 , and 6.8 moles of NOCl are mixed in a 2.0–L flask.

In which direction will the system proceed to reach equilibrium?



EXAMPLE - 11

ANS:



$$K_c = 6.5 \times 10^4$$

$$Q_c = \frac{[\text{NOCl}]^2}{[\text{NO}]^2 [\text{Cl}_2]}$$

Initial concentrations:

$$\begin{aligned} [\text{NOCl}_2] &= \frac{6.8 \text{ mol}}{2.0 \text{ L}} \\ &= 3.4 \text{ M} \end{aligned}$$

$$[\text{NO}] = \frac{2.0 \times 10^{-2} \text{ mol}}{2.0 \text{ L}}$$

$$= 0.01 \text{ M}$$

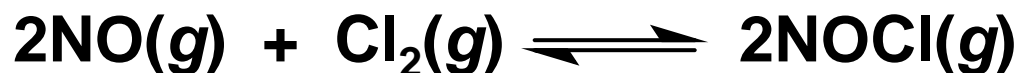
$$[\text{Cl}_2] = \frac{8.3 \times 10^{-3} \text{ mol}}{2.0 \text{ L}}$$

$$= 0.0042 \text{ M}$$



EXAMPLE - 11

ANS:



$$K_C = 6.5 \times 10^4$$

Initial concentrations:

$$[\text{NOCl}_2] = 3.4 \text{ M}$$

$$[\text{NO}] = 0.01 \text{ M}$$

$$[\text{Cl}_2] = 0.0042 \text{ M}$$

$$Q_C = \frac{[\text{NOCl}]^2}{[\text{NO}]^2 [\text{Cl}_2]}$$
$$= \frac{3.4^2}{0.01^2 \times 0.0042}$$
$$= 2.75 \times 10^7$$

$$Q_C > K_C$$
$$(2.75 \times 10^7) > (6.5 \times 10^4)$$

Numerator (products)
is **larger** than
denominator (reactants)

The reaction is not at equilibrium and will proceed to the left until $Q_C = K_C$.

Summary of the steps involved in solving equilibrium problems

PRELIMINARY SETTING UP

1. Write the balanced equation
2. Write the reaction quotient, Q
3. Convert all amounts into the correct units (M or atm)

WORKING ON THE REACTION TABLE

4. When reaction direction is not known, compare Q with K
5. Construct a reaction table

✓ Check the sign of x , the change in the quantity

SOLVING FOR x AND EQUILIBRIUM QUANTITIES

6. Substitute the quantities into Q
7. To simplify the math, assume that x is negligible
($[A]_{\text{init}} - x = [A]_{\text{eq}} \approx [A]_{\text{init}}$)
8. Solve for x

✓ Check that assumption is justified ($< 5\%$ error). If not, solve quadratic equation for x .

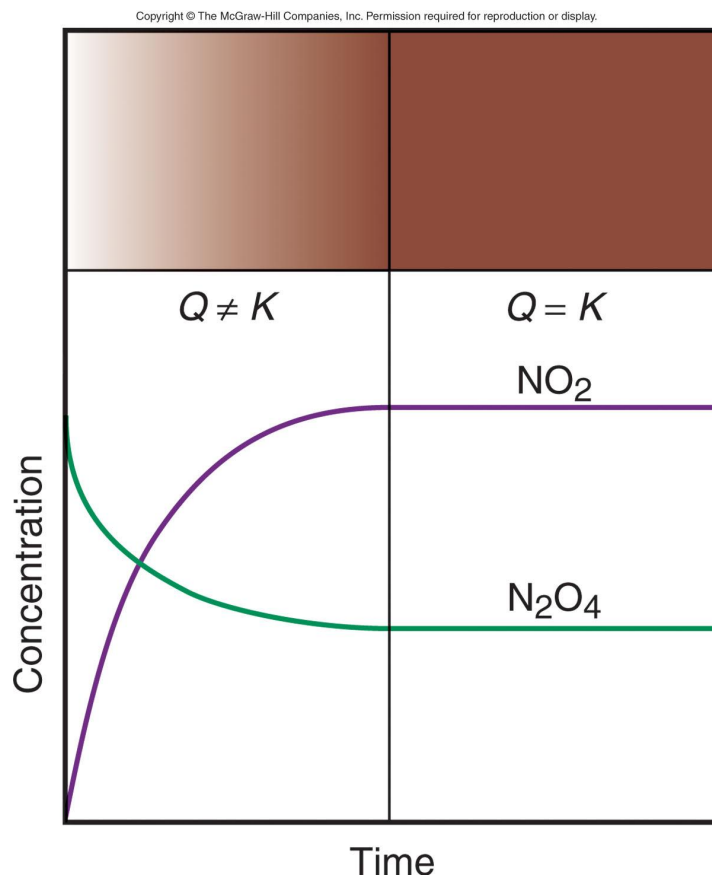
9. Find the equilibrium quantities

✓ Check to see that calculated values give the known K



EXERCISE - 45

State three criteria that characterize a chemical system that characterize a chemical system at equilibrium.



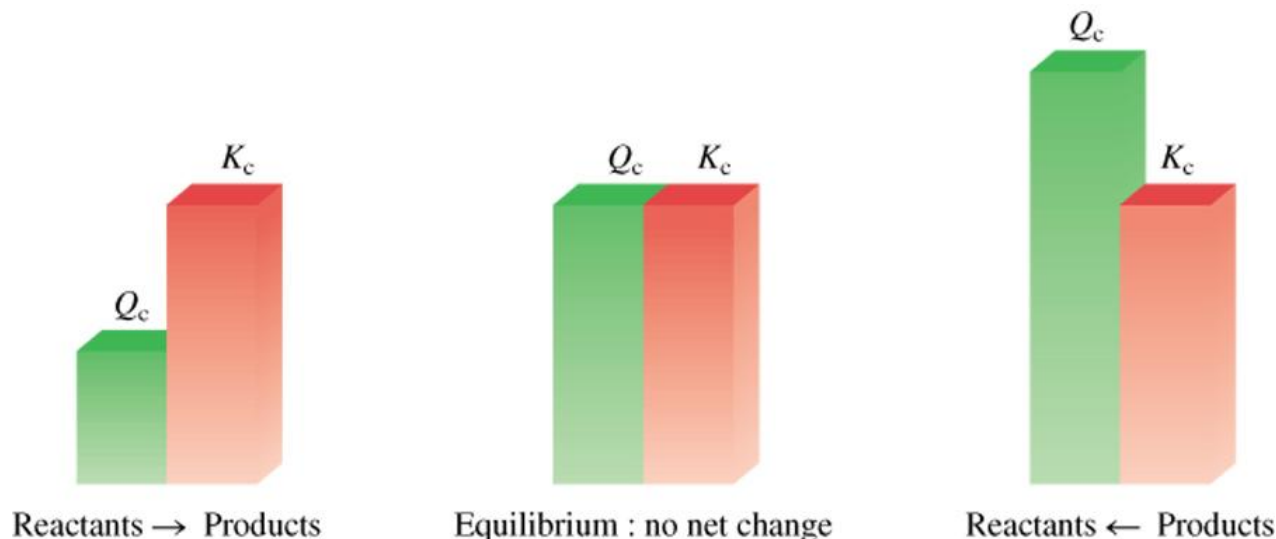


EXERCISE - 46

State the reaction $\text{N}_2\text{O}_4(\text{g}) \rightleftharpoons 2\text{NO}_2(\text{g})$,
 $K_c = 0.21$ at 100°C . At a point during the reaction,
 $[\text{N}_2\text{O}_4] = 0.12 \text{ M}$ and $[\text{NO}_2] = 0.55 \text{ M}$.

Is the reaction at equilibrium?

If not, in which direction is it progressing?





EXERCISE - 47

Chloromethane forms by the reaction

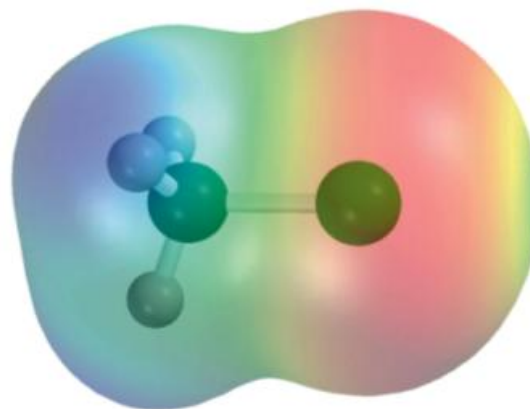


At 1500 K, $K_p = 1.6 \times 10^4$. In the reaction mixture,

$P_{\text{CH}_4} = 0.13 \text{ atm}$, $P_{\text{Cl}_2} = 0.035 \text{ atm}$

$P_{\text{CH}_3\text{Cl}} = 0.24 \text{ atm}$, and $P_{\text{HCl}} = 0.47 \text{ atm}$.

Is CH_3Cl or CH_4 forming?



Chloromethane (CH_3Cl)



EXERCISE - 48

At the start of a reaction, there are 0.249 mol N_2 , 3.21×10^{-2} mol H_2 , and 6.42×10^{-4} mol NH_3 in a 3.50-L reaction vessel at 375°C .

If K_C for the reaction



is 1.2 at this temperature, decide whether the system is at equilibrium.

If not, predict which way the net reaction will proceed.



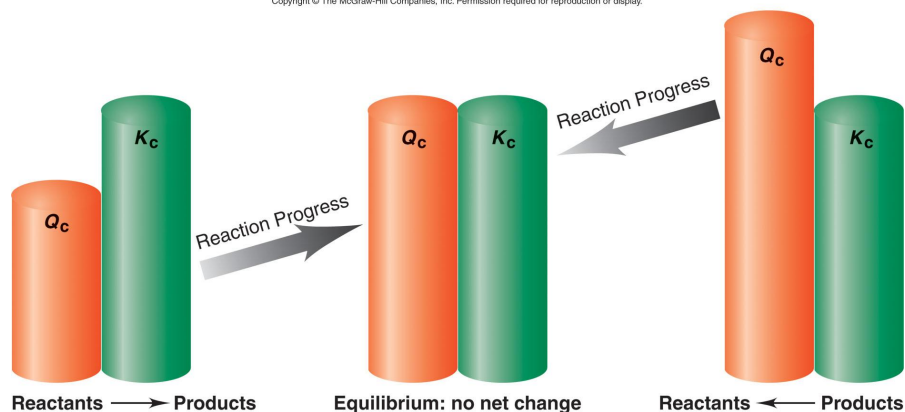
EXERCISE - 49

For the synthesis of ammonia



K_c at 375°C is 1.2. Starting with $[\text{H}_2] = 0.76 \text{ M}$, $[\text{N}_2] = 0.60 \text{ M}$, $[\text{NH}_3] = 0.48 \text{ M}$, which gases will increased in concentration and which will have decreased in concentration when the mixture comes to equilibrium?

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EXERCISE - 50

At 425°C, $K_p = 4.18 \times 10^{-9}$ for the reaction



In one experiment, 0.20 atm of $\text{HBr}(g)$, 0.010 atm of $\text{H}_2(g)$, and 0.010 atm of $\text{Br}_2(g)$ are introduced into a container.

Is the system at equilibrium?

If not, in which direction will it proceed?



EXERCISE - 51

At 100°C , $K_p = 60.6$ for the reaction



In a given temperature, 0.10 atm of each component is placed in a container.

Is the reaction at equilibrium?

If not, in which direction will it proceed?



EXERCISE - 52

The water–gas shift reaction plays a central role in the chemical methods for obtaining cleaner fuels from coal:



In a given temperature, $K_p = 2.7$.

If 0.13 mol of CO, 0.56 mol of H₂O, 0.62 mol of CO₂, and 0.43 mol of H₂ are introduced into a 2.0–L flask, in which direction must the reaction proceed to reach equilibrium?





*END OF
SLIDE SHOW*

